

1 The diagram shows an isosceles triangle.

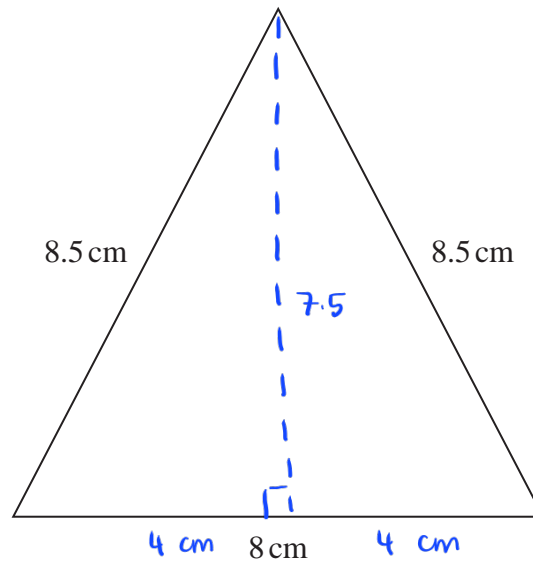
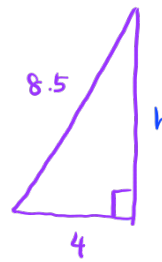


Diagram **NOT**
accurately drawn

Work out the area of the triangle.

By using Pythagoras' Theorem :

$$\begin{aligned} h &= \sqrt{8.5^2 - 4^2} \\ &= \sqrt{56.25} \text{ ①} \\ &= 7.5 \text{ cm ①} \end{aligned}$$



Area of triangle : $\frac{1}{2} \times \text{base} \times \text{height}$

$$= \frac{1}{2} \times 8 \text{ cm} \times 7.5 \text{ cm ①}$$

$$= 30 \text{ cm}^2 \text{ ①}$$

30

.....cm²

(Total for Question 1 is 4 marks)

2 The diagram shows a triangle.

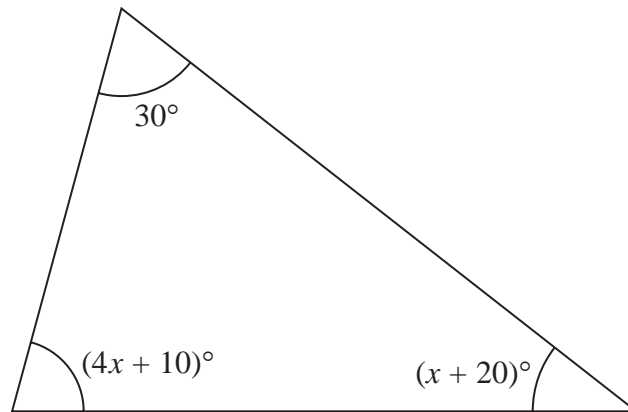


Diagram **NOT**
accurately drawn

Work out the value of x . (Angles in a triangle sums up to 180°)

$$30^\circ + (4x + 10)^\circ + (x + 20)^\circ = 180^\circ$$

$$5x + 30 + 30 = 180$$

$$5x + 60 = 180 \quad \textcircled{1}$$

$$5x = 180 - 60 \quad \textcircled{1}$$

$$5x = 120 \quad \textcircled{1}$$

$$x = \frac{120}{5} \quad \textcircled{1}$$

$$= 24 \quad \textcircled{1}$$

$$x = \dots\dots\dots 24$$

(Total for Question 2 is 4 marks)

3 The diagram shows the isosceles triangle ABC in which $AB = AC$

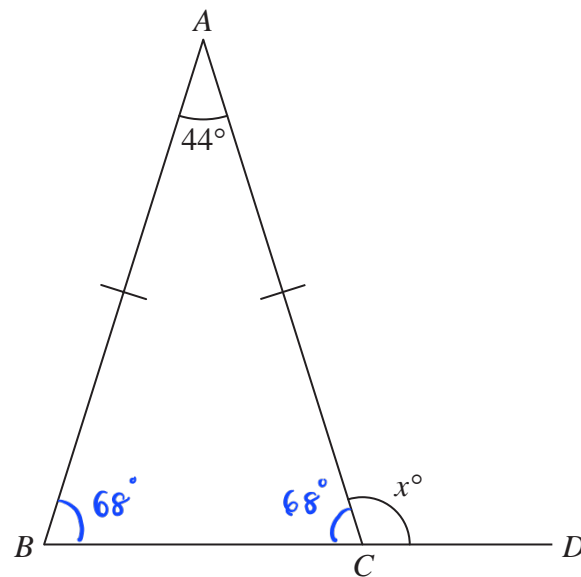


Diagram **NOT**
accurately drawn

BCD is a straight line.

Work out the value of x .

$$\begin{aligned} \text{angle } ABC &= \text{angle } ACB = \frac{180^\circ - 44^\circ}{2} && \text{- base angles of isosceles triangles} \\ &= 68^\circ \text{ (1)} && \text{are the same} \end{aligned}$$

$$\begin{aligned} x &= 180^\circ - 68^\circ \text{ (1)} \\ &= 112^\circ \text{ (1)} \end{aligned}$$

$$x = \underline{\underline{112}}$$

(Total for Question 3 is 3 marks)

4 Here is isosceles triangle ABC .

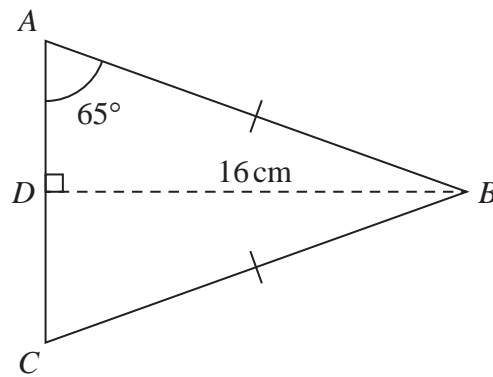


Diagram **NOT**
accurately drawn

D is the midpoint of AC and $DB = 16$ cm.

Angle $DAB = 65^\circ$

Work out the perimeter of triangle ABC .
Give your answer correct to one decimal place.

$$AD = \frac{16}{\tan 65^\circ} \quad (1)$$

$$= 7.4609 \dots \text{ cm}$$

$$AB = \frac{16}{\sin 65^\circ}$$

$$= 17.654 \dots \text{ cm} \quad (1)$$

$$\text{Perimeter} = 2(17.654 \dots) + 2(7.4609 \dots) \quad (1)$$

$$= 50.2 \text{ cm (1dp)} \quad (1)$$

50.2 cm

(Total for Question 4 is 4 marks)

5 A , B and C are points on a circle with centre O .

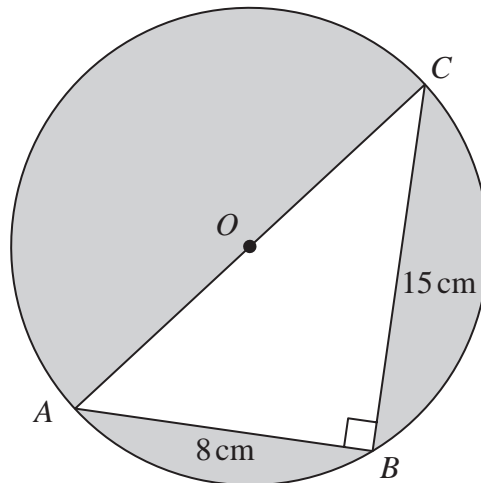


Diagram **NOT**
accurately drawn

AOC is a diameter of the circle.

$AB = 8\text{ cm}$ $BC = 15\text{ cm}$

Angle $ABC = 90^\circ$

Work out the total area of the regions shown shaded in the diagram.
Give your answer correct to 3 significant figures.

$$\text{Area of triangle} = \frac{1}{2} ab \sin C$$

$$\begin{aligned} \text{Area of triangle} &= \frac{1}{2} \times 8 \times 15 \times \sin 90^\circ \\ &= 60 \end{aligned}$$

$$\begin{aligned} AC &= \sqrt{8^2 + 15^2} \quad (1) \\ &= 17 \quad (1) \end{aligned}$$

$$\text{radius of circle} = 17 \div 2 = 8.5\text{ cm}$$

$$\begin{aligned} \text{Area of circle} &= \pi r^2 \\ &= \pi (8.5)^2 \\ &= 226.98 \quad (1) \end{aligned}$$

$$\begin{aligned} \text{Area of shaded region} &= 226.98 - 60 \quad (1) \\ &= 166.98 \\ &= 167 \text{ (3sf)} \quad (1) \end{aligned}$$

167

.....cm²

(Total for Question 5 is 5 marks)

- 6 The diagram shows a shape $ABCDEFG$ made from a square $ABDF$ and three identical isosceles triangles BCD , DEF and FGA .

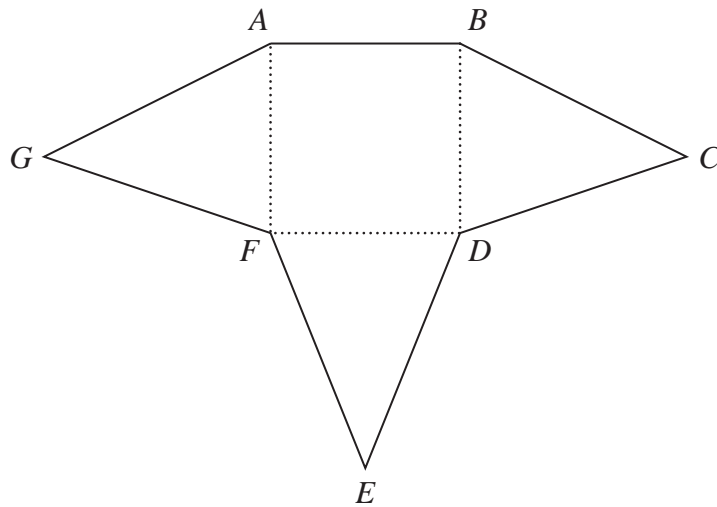


Diagram **NOT**
accurately drawn

The perimeter of the square $ABDF$ is 48 cm.
The perimeter of each isosceles triangle is 30 cm.

Work out the perimeter of the shape $ABCDEFG$.

$$\text{length } AB : \frac{48}{4} = 12 \text{ cm} \quad (1)$$

$$\text{length } AG : \frac{30 - 12}{2} = 9 \text{ cm} \quad (1)$$

$$\text{Perimeter} : (6 \times 9) + 12$$

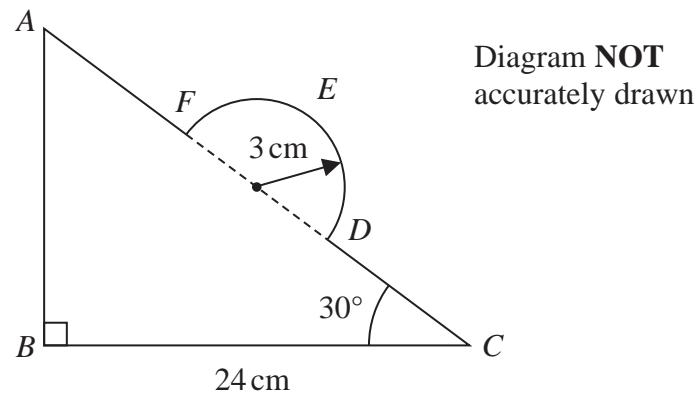
$$: 54 + 12 \quad (1)$$

$$: 66 \text{ cm} \quad (1)$$

..... 66 cm

(Total for Question 6 is 4 marks)

7 In the diagram, ABC is a right-angled triangle and DEF is a semicircular arc.



In triangle ABC

$$BC = 24 \text{ cm}$$

$$\text{angle } ABC = 90^\circ$$

$$\text{angle } BCA = 30^\circ$$

The points D and F lie on AC so that DF is the diameter of the semicircular arc DEF .
The radius of the semicircular arc is 3 cm.

Work out the length of $AFEDC$

Give your answer correct to 2 significant figures.

$$\cos 30^\circ = \frac{24}{AC} \quad (1)$$

$$AC = \frac{24}{\cos 30^\circ} = 27.712 \dots \quad (1)$$

$$FED = \frac{1}{2} \times 2 \times \pi \times 3 \quad (1)$$

$$= 3\pi = 9.424 \dots$$

$$AFEDC = 27.712 - 3 - 3 + 9.424 \quad (1)$$

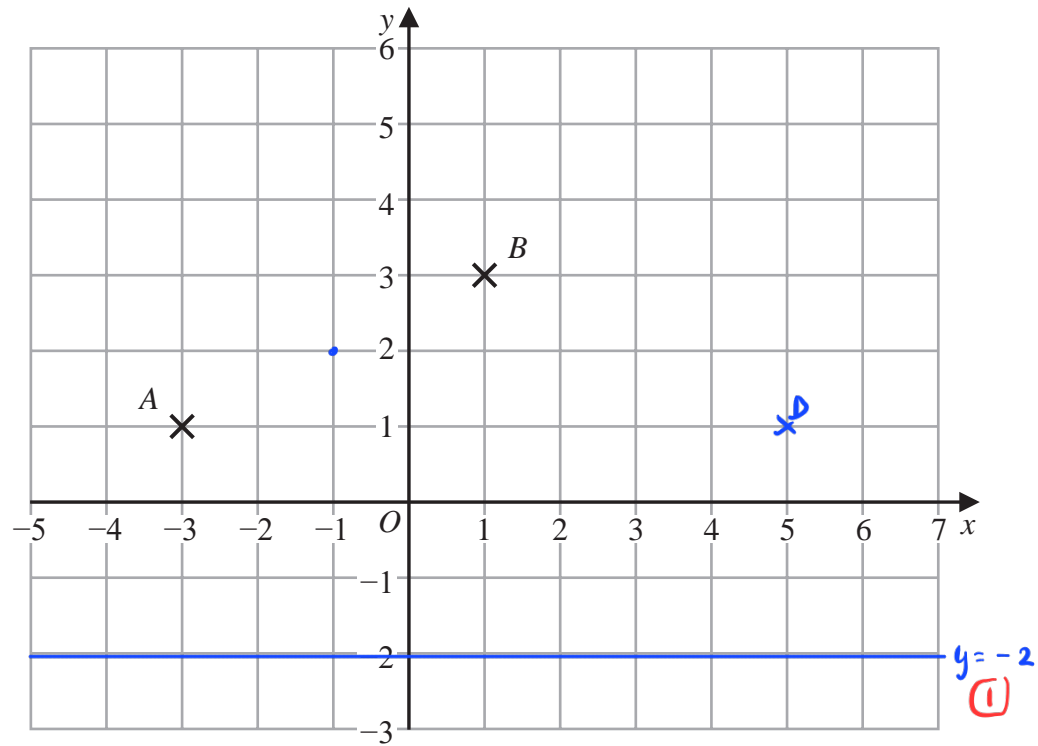
$$= 31 \quad (1)$$

31

..... cm

(Total for Question 7 is 5 marks)

- 8 The diagram shows points A and B marked on a grid of squares.



D is the point with coordinates $(5, d)$ where $d > 0$
 The triangle ABD is an isosceles triangle.

- (c) Find the value of d

$d =$ 1 (1)

(Total for Question 8 is 1 marks)

9

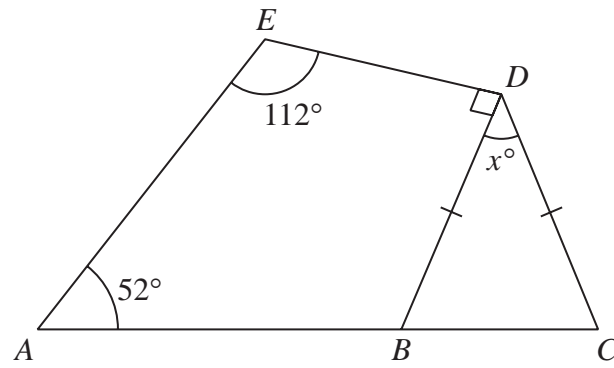


Diagram **NOT**
accurately drawn

BCD is an isosceles triangle with $BD = CD$

ABC is a straight line.

$ABDE$ is a quadrilateral.

Work out the value of x

Give a reason for each stage of your working.

$$\text{ABD} = 360 - 52 - 112 - 90$$

$$= 106 \quad (1)$$

(angles in a quadrilateral add up to 360°) (1)

$$\text{CBD} = 180 - 106$$

$$= 74 \quad (1)$$

(angles on a straight line add to 180°)

$$x = 180^\circ - 2(74^\circ) \quad \text{— (base angles in isosceles are equal)}$$

$$= 180^\circ - 148^\circ$$

$$= 32^\circ \quad (1)$$

$$x = \underline{\quad 32 \quad}$$

(Total for Question 9 is 4 marks)

10 The diagram shows an isosceles triangle ABC

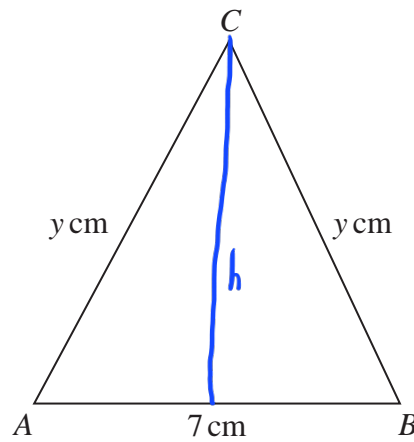


Diagram **NOT**
accurately drawn

$$AB = 7\text{ cm} \quad AC = BC = y\text{ cm}$$

The area of the triangle is 42 cm^2

Work out the value of y

$$\text{Area} : \frac{1}{2} \times 7 \times h = 42$$

$$h = 12 \quad (1)$$

$$y^2 = 12^2 + 3.5^2 \quad (1)$$

$$y = \sqrt{12^2 + 3.5^2} \quad (1)$$

$$= 12.5 \quad (1)$$

$$y = \underline{\underline{12.5}}$$

(Total for Question 10 is 4 marks)

11 The diagram shows quadrilateral $ABCD$

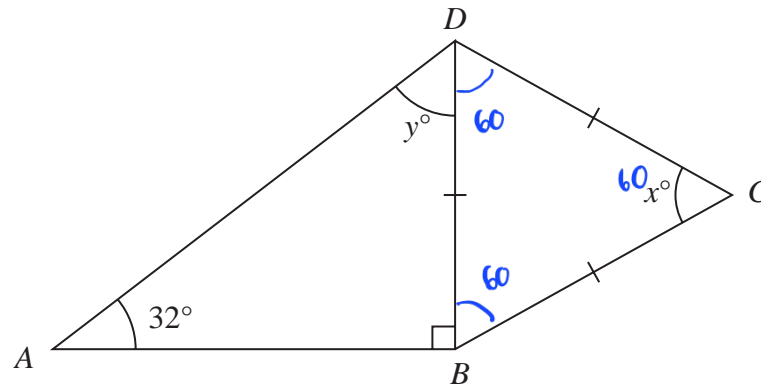


Diagram **NOT**
accurately drawn

$$BC = CD = DB$$

angle $DBA = 90^\circ$ and angle $DAB = 32^\circ$

(a) Work out the value of x

$$x = \frac{60}{1} \quad (1)$$

(b) (i) Work out the value of y

$$180 - 90 - 32 = 58$$

$$y = \frac{58}{1} \quad (1)$$

(ii) Give a reason for your answer to (b)(i).

Angles in a triangle add up to 180° (1)

(1)

(Total for Question 11 is 3 marks)